

Algebraic Geometry 2^{1/2} supplementary worksheet 6

Domination, dominant maps, valuation rings

Critical Hartshorne problems in Chapter II

- (short term) 3.17, 3.18
 - (longer term) 3.19, 3.22
1. A morphism of schemes $X \rightarrow Y$ is called dominant if it has dense image. A good source for this is the stacks project <https://stacks.math.columbia.edu/tag/01RI>. Take a look at the following facts from there:
 1. Morphisms whose image contains the generic points are dominant (Tag 01RL)
 2. Ring maps have dense Zariski images if their kernels are radical (Lemma 00FL)